

# Everything is a tradeoff

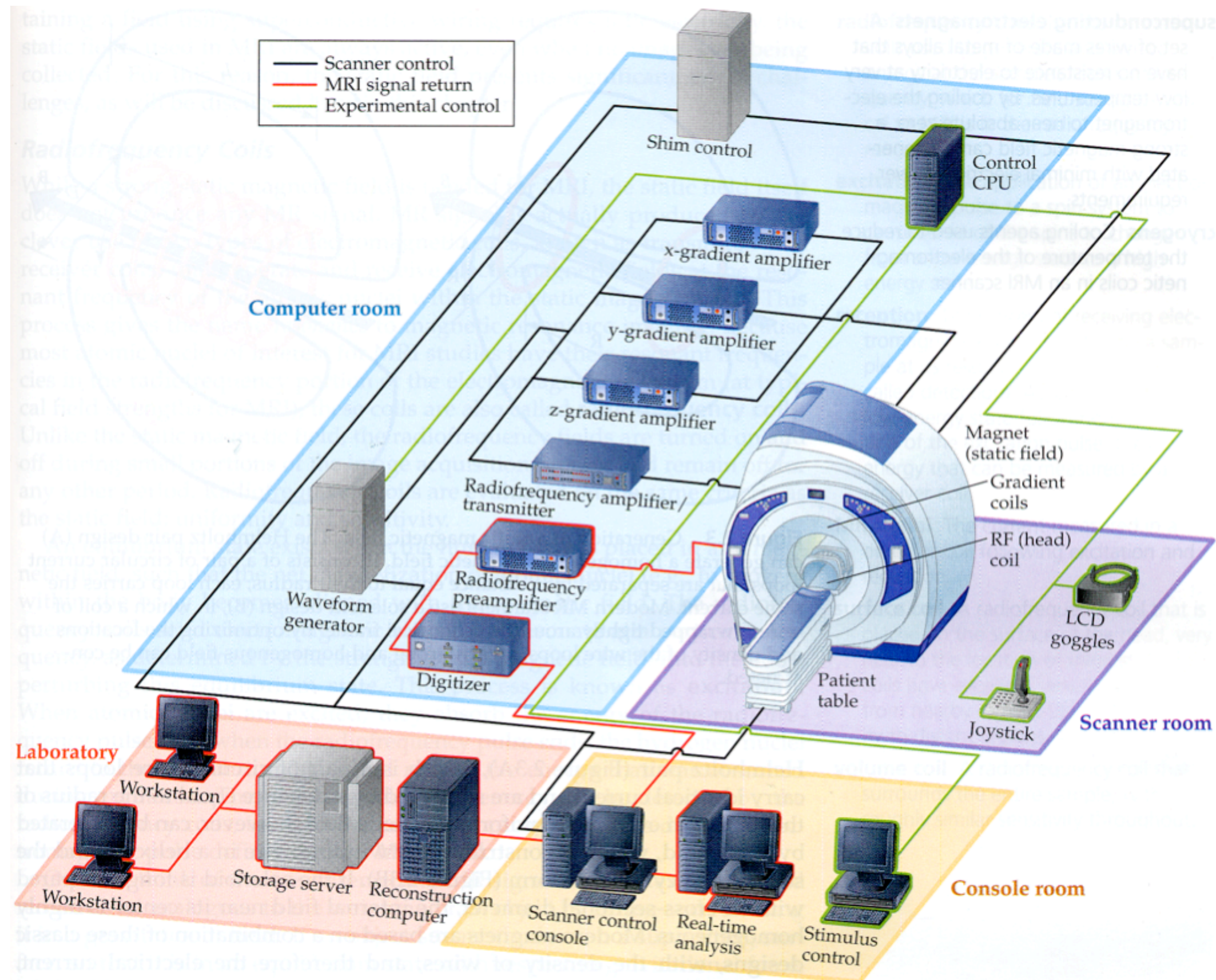
Souheil Inati  
FMRI Course  
July 1, 2011

Interrupt early and often.

**Nothing is free**

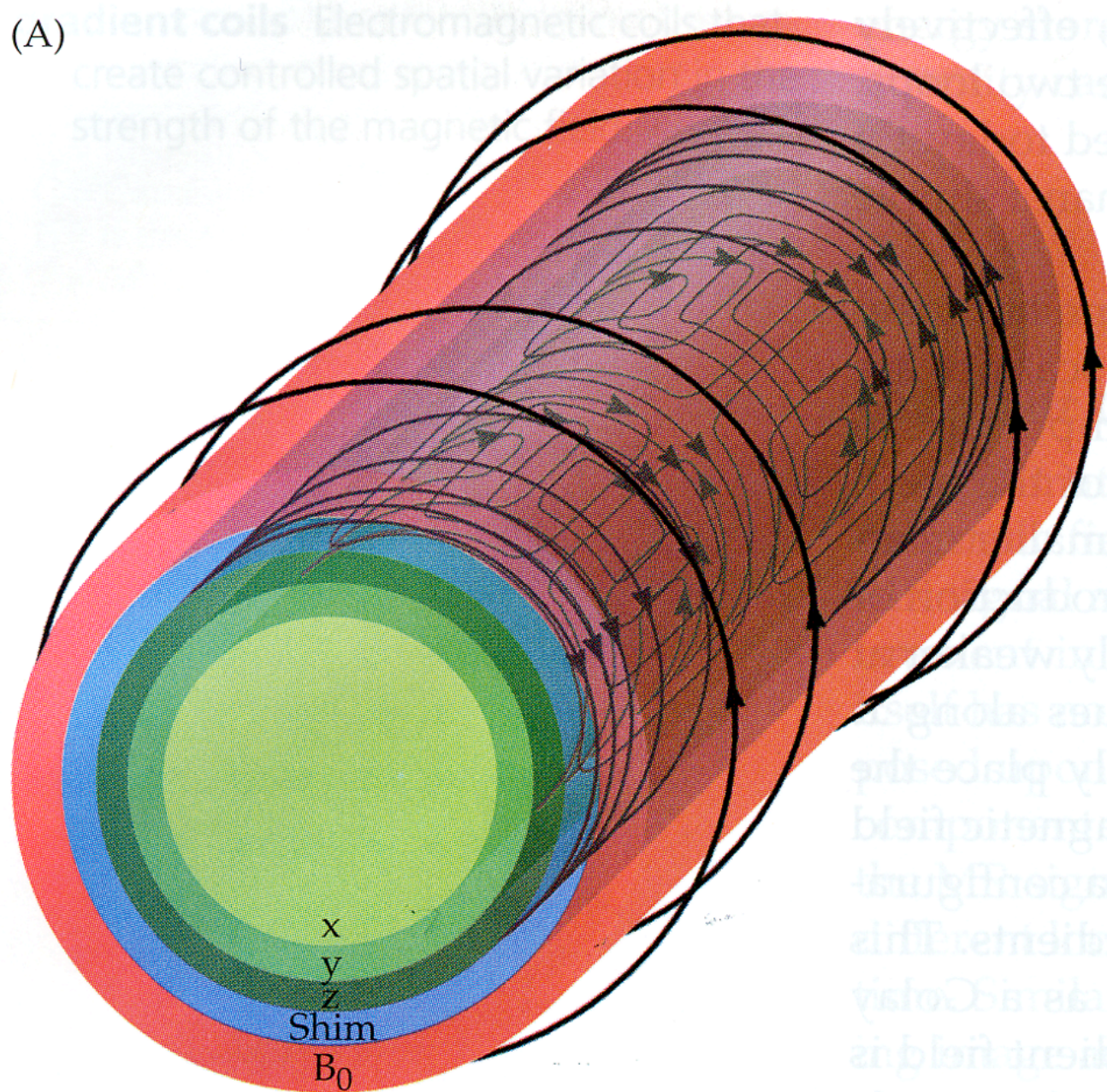
**fast, good, cheap  
... chose two**

# The Hardware





# Magnet and Gradients

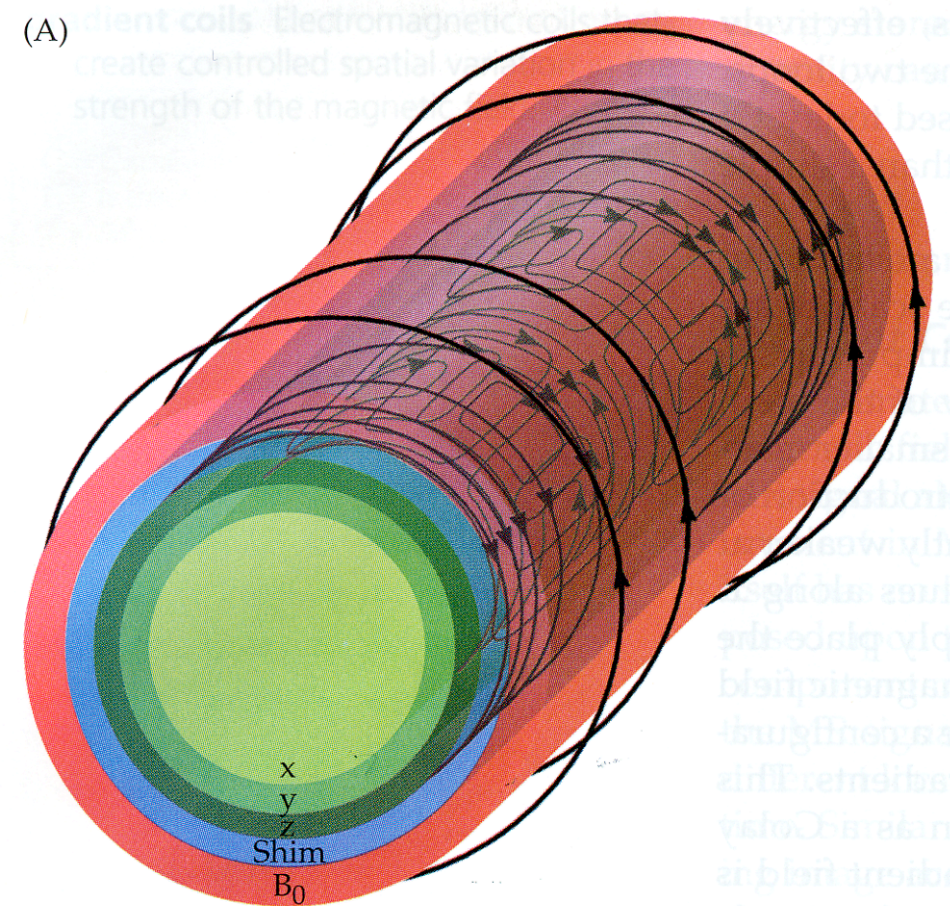
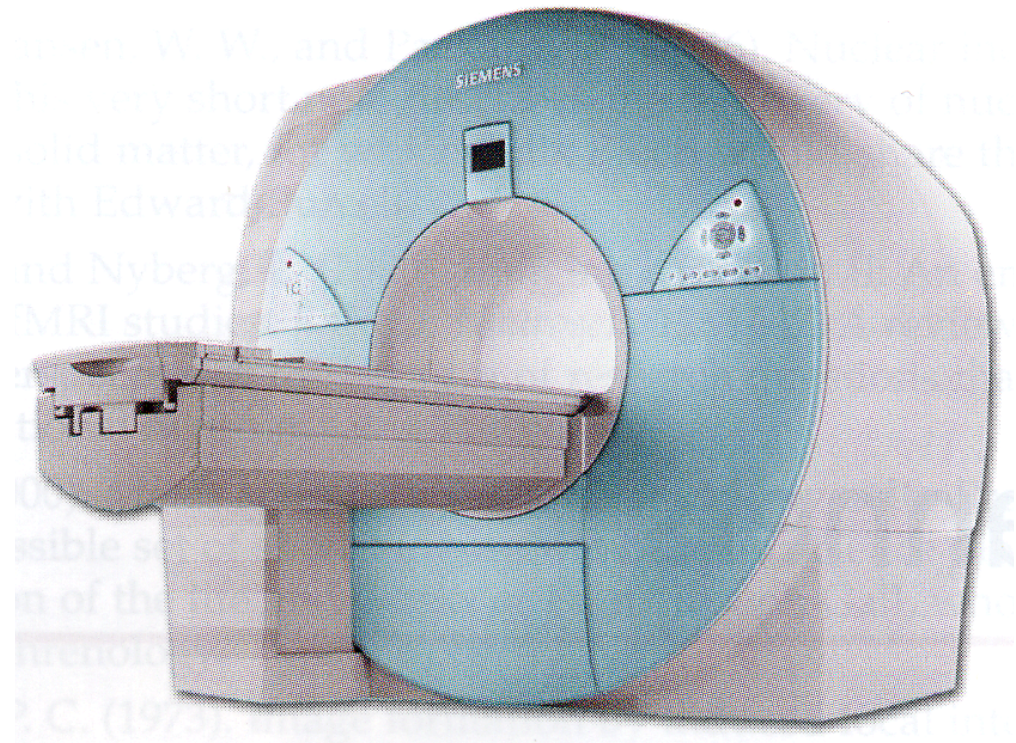




# Magnet

- field strength
- bore size
- length/weight
- self-shielded
- homogeneity/shims
- helium boiloff

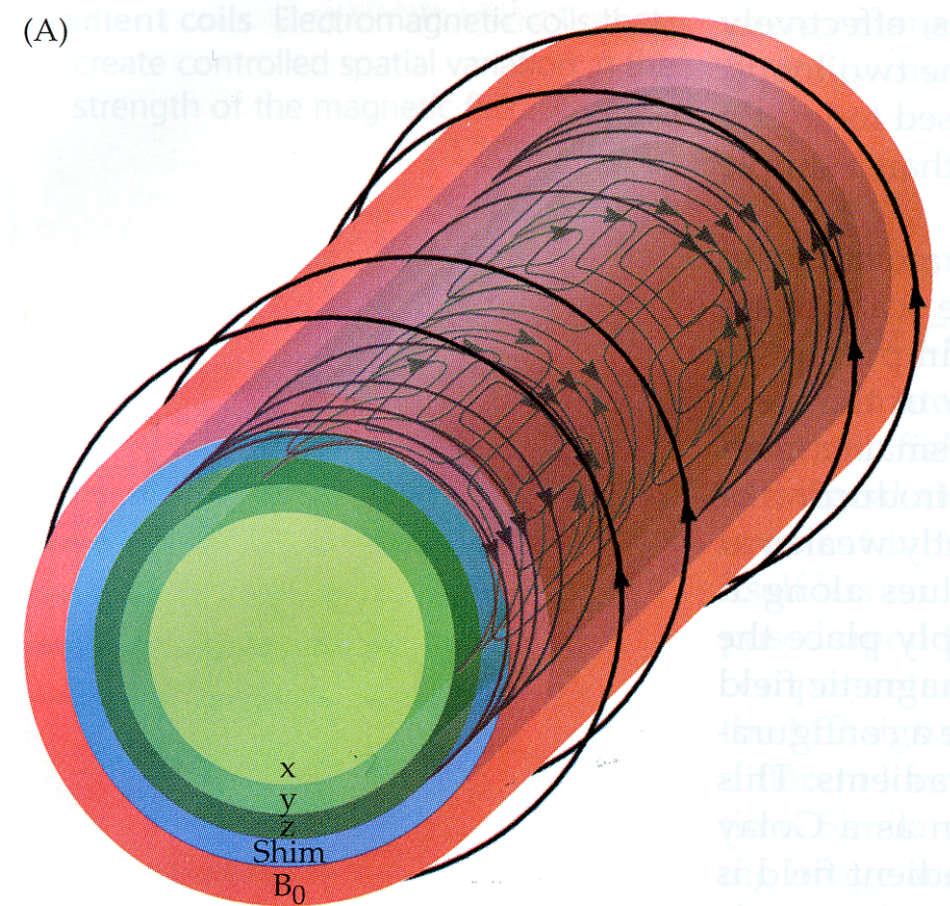
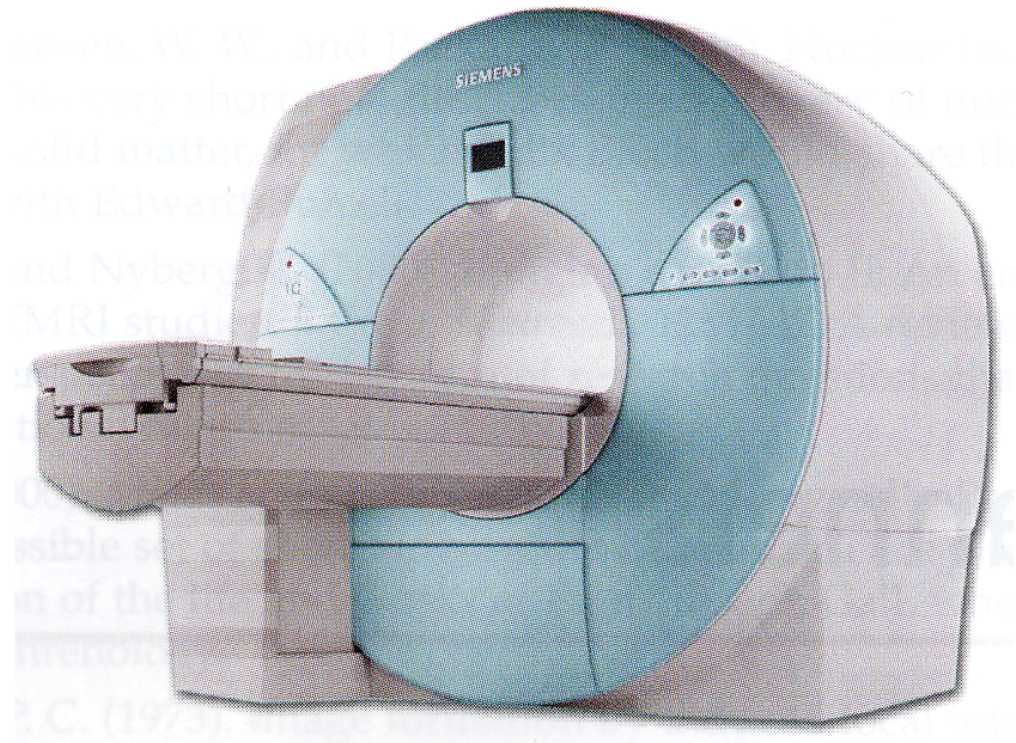
**\$1,000,000/Tesla**





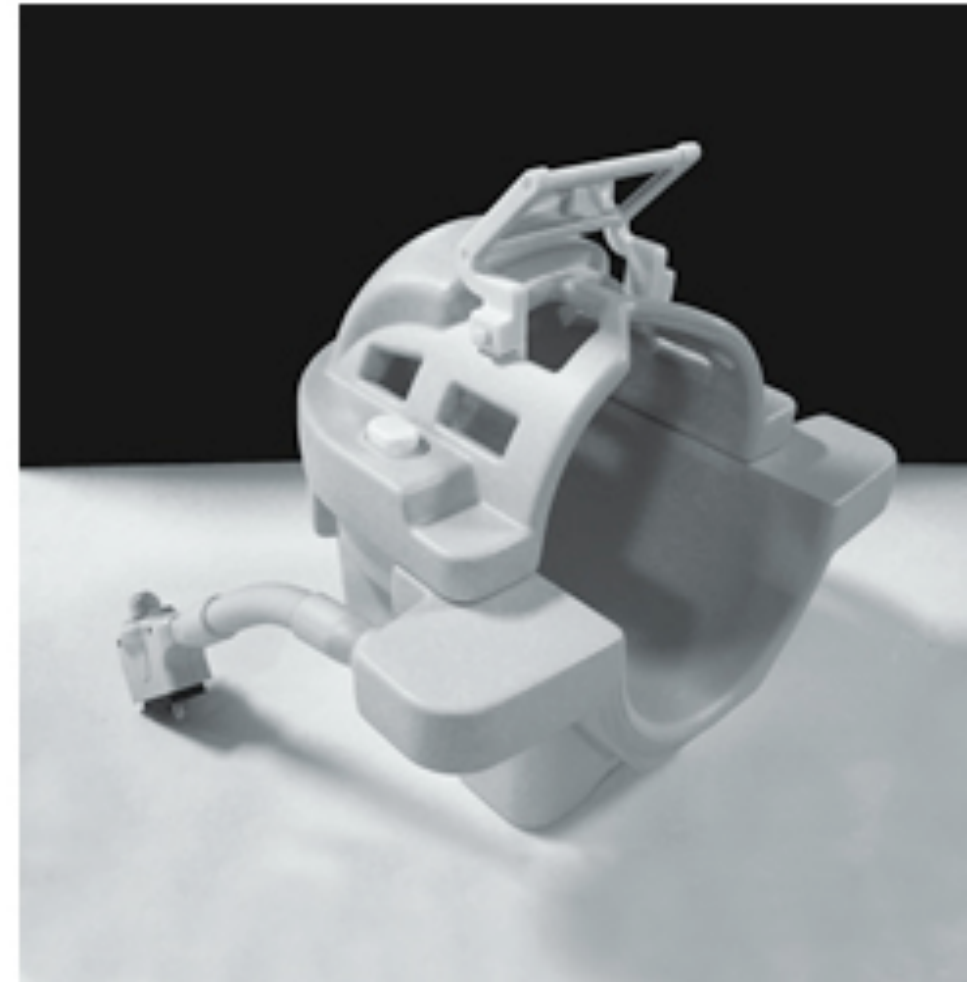
# Gradients

- size (head/body)
- strength
- slew rate
- duty cycle
- linearity
- eddy currents
- water cooling
- vibration/acoustics



# RF Coils

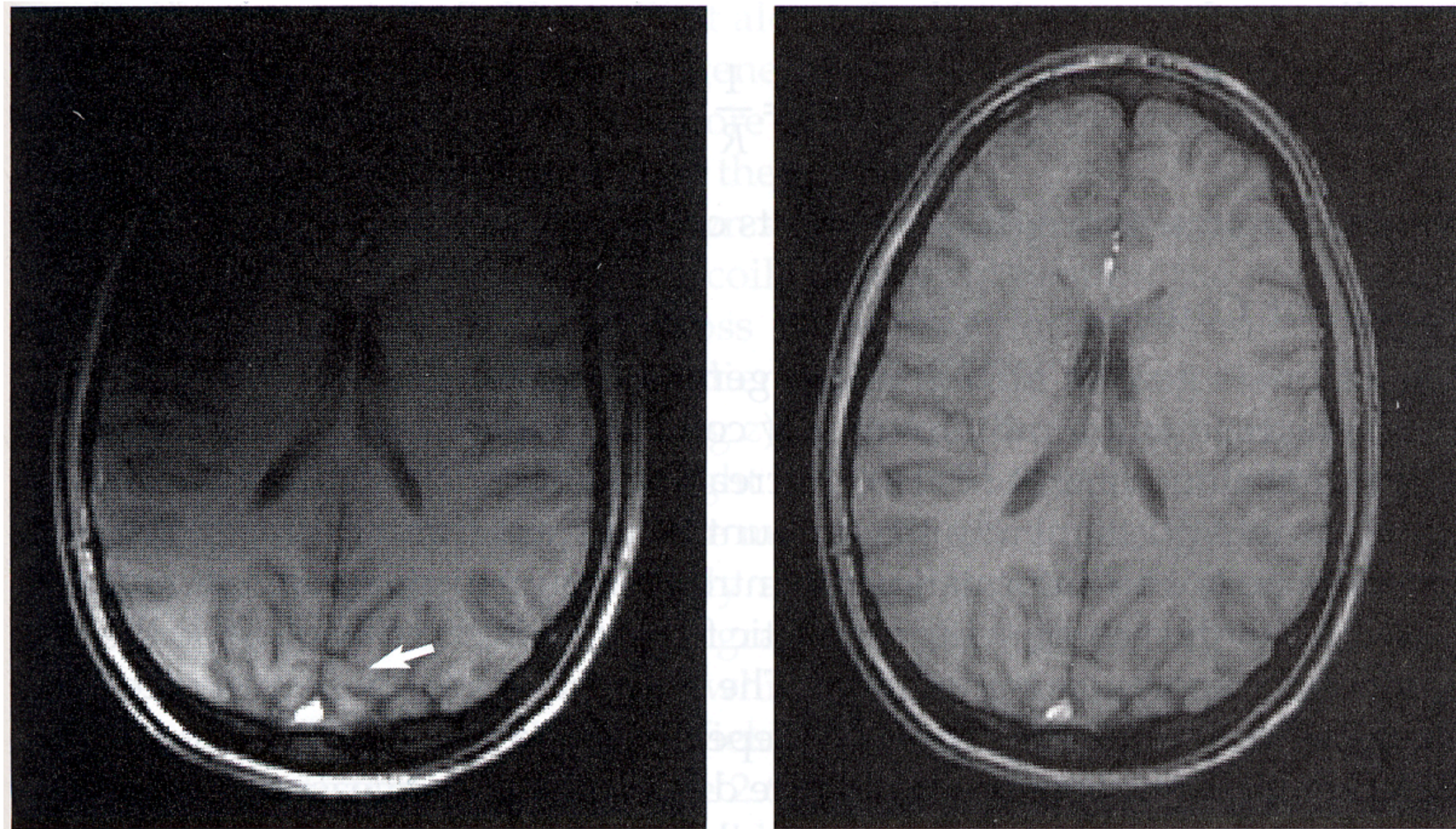
- Receive coil
  - size/shape/coverage
  - element # and arrangement
  - mechanical design/robustness
- Transmit coil
  - head/body Tx
  - multi-channel Tx
- FDA Approval, warrantee and service



3T 32 channel head  
Rx array \$80k



# Surface Coils vs Volume Coils



Tradeoff uniformity for increased SNR locally



# Amplifiers

- Lots of Amps
  - Shims
  - Gradients
  - RF Transmit
  - RF Receive
- Issues
  - gain
  - noise figure
  - stability
  - duty cycle

Tradeoffs - each optimized differently

# Digitizers, computers

- Digital to Analog
  - Gradients, RF waveforms
- Analog to Digital
  - RF Receiver
  - Physiology monitors
  - Sensors (Temp, Flow)
- Computers
  - sequencer, embedded monitors, recon engine
- Optimization Criteria
  - Dynamic range
  - Fidelity (Accuracy)
  - Speed
  - Hardware architecture
    - CPU speed, RAM
  - Software architecture
    - real-time, parallel

# Ancillary equipment

- Projectors
  - resolution, color, speed
  - lens system optics throw, image size
- Interface devices
  - mechanical design/robustness
  - ease of use with stimulus programs
- Physiological monitoring
- Eye-tracking, EMG, EEG, ...
- FDA Approval, warrantee and service



~~fast, good, cheap  
... chose two~~

**SPEED KILLS**

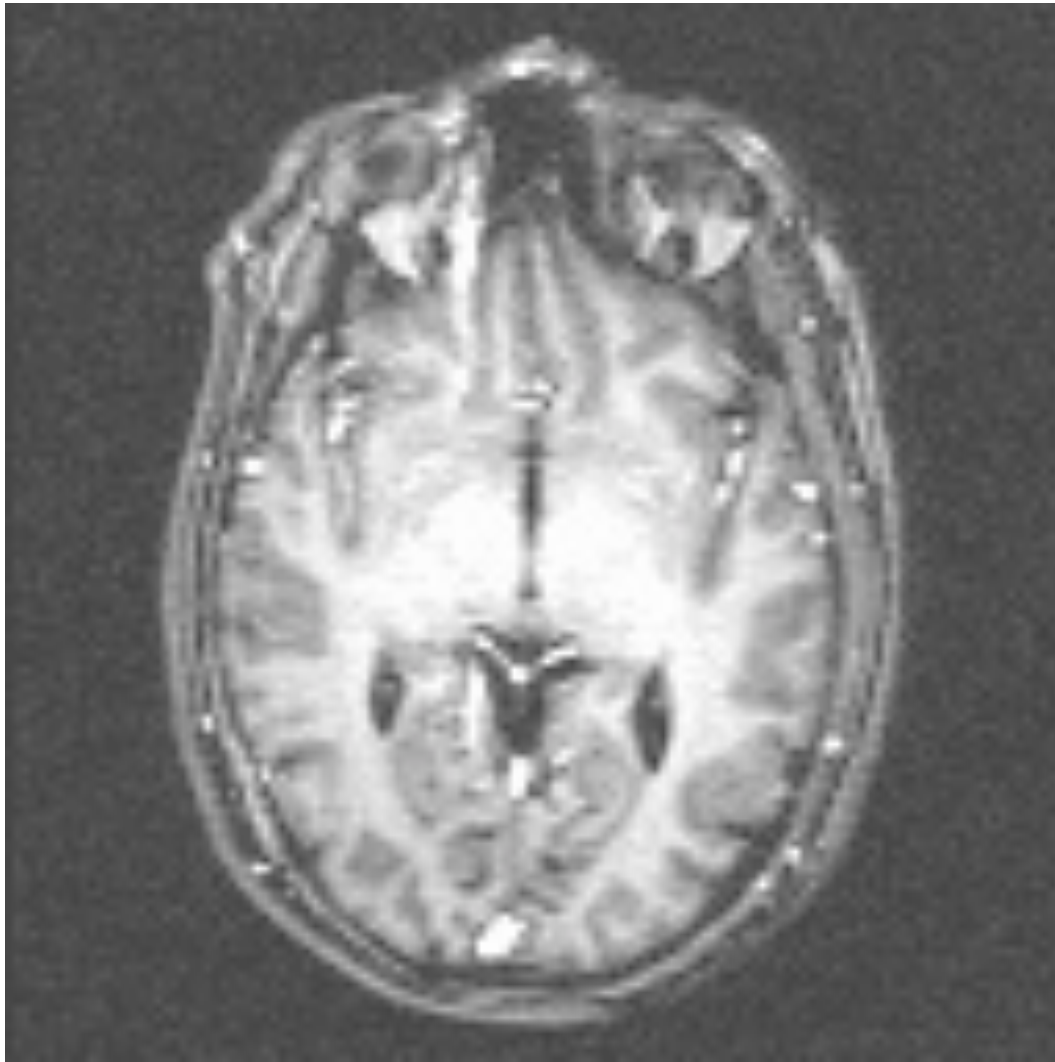
speed vs image artifacts

speed vs coverage

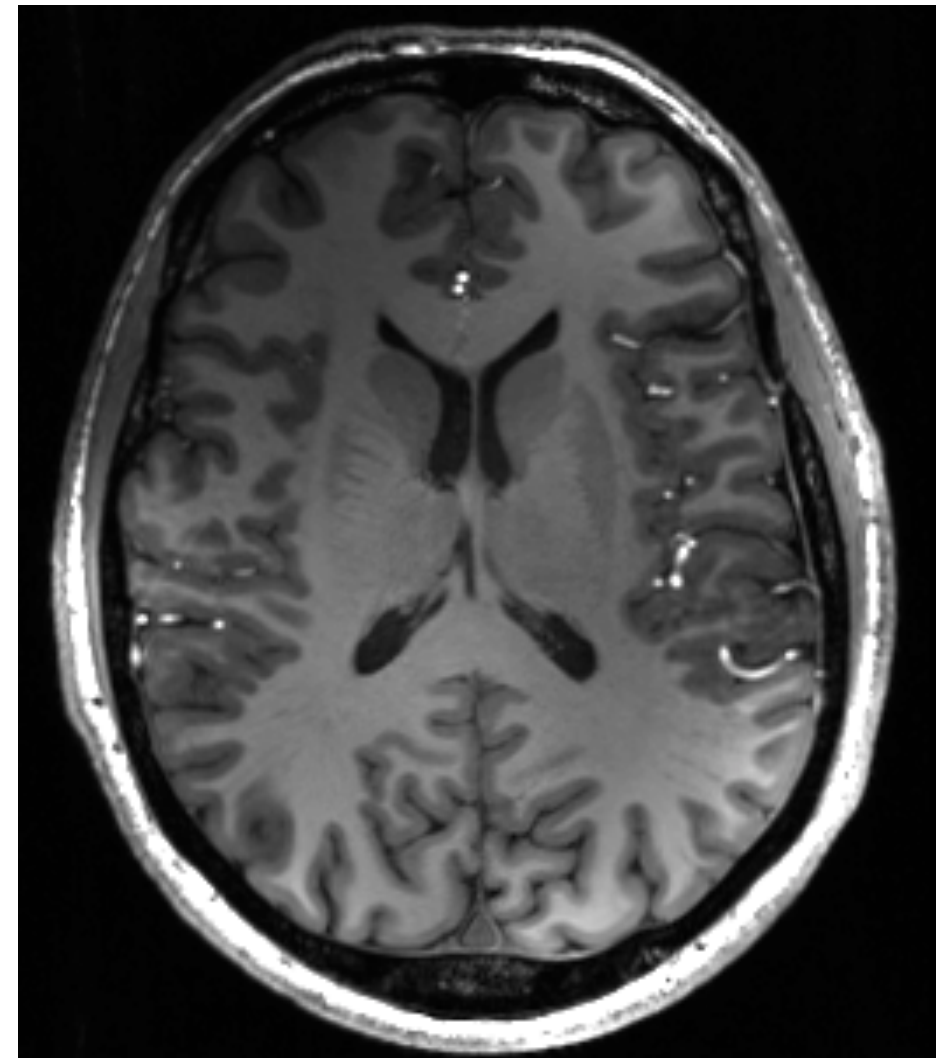
speed vs resolution

speed vs signal to noise ratio

# Hardware Matters



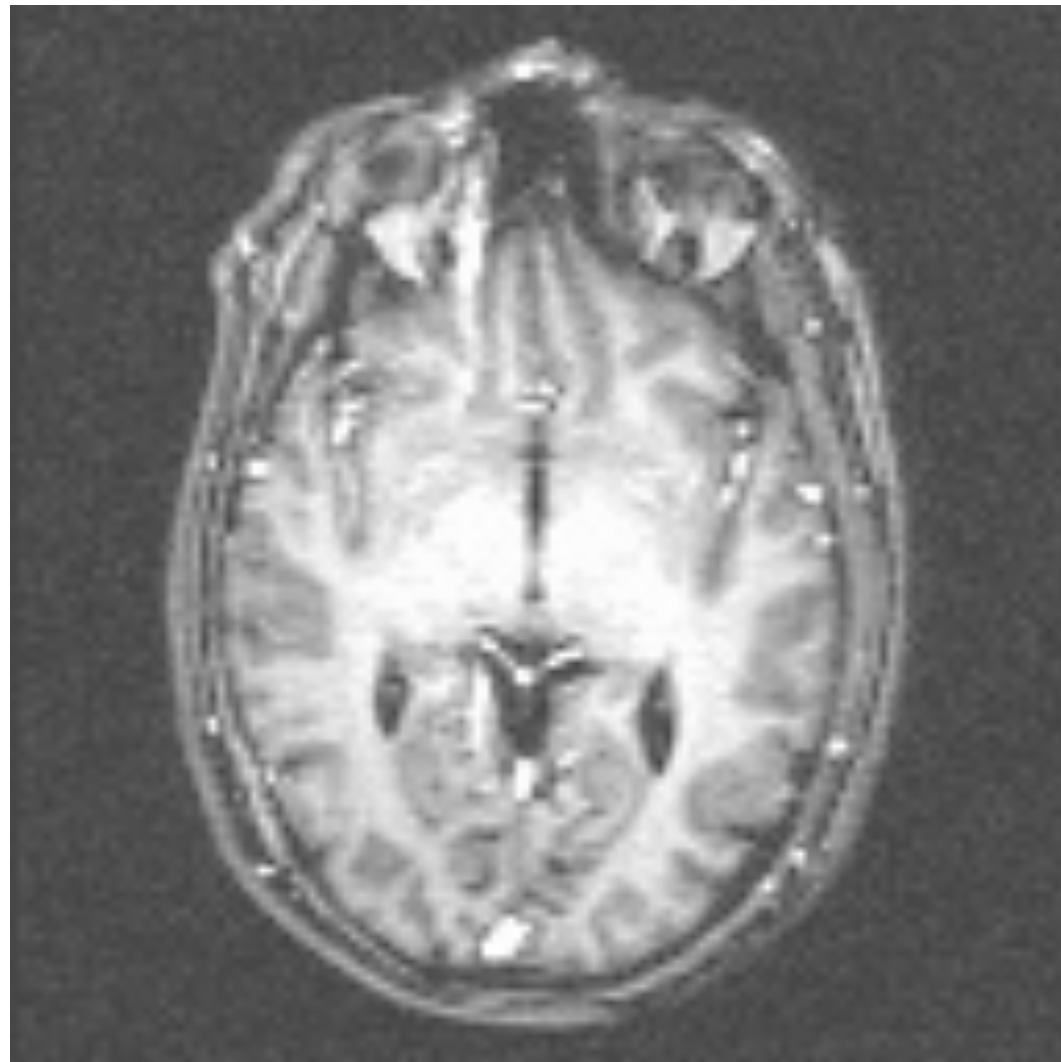
1 mm, 10 min  
3T, Volume Coil



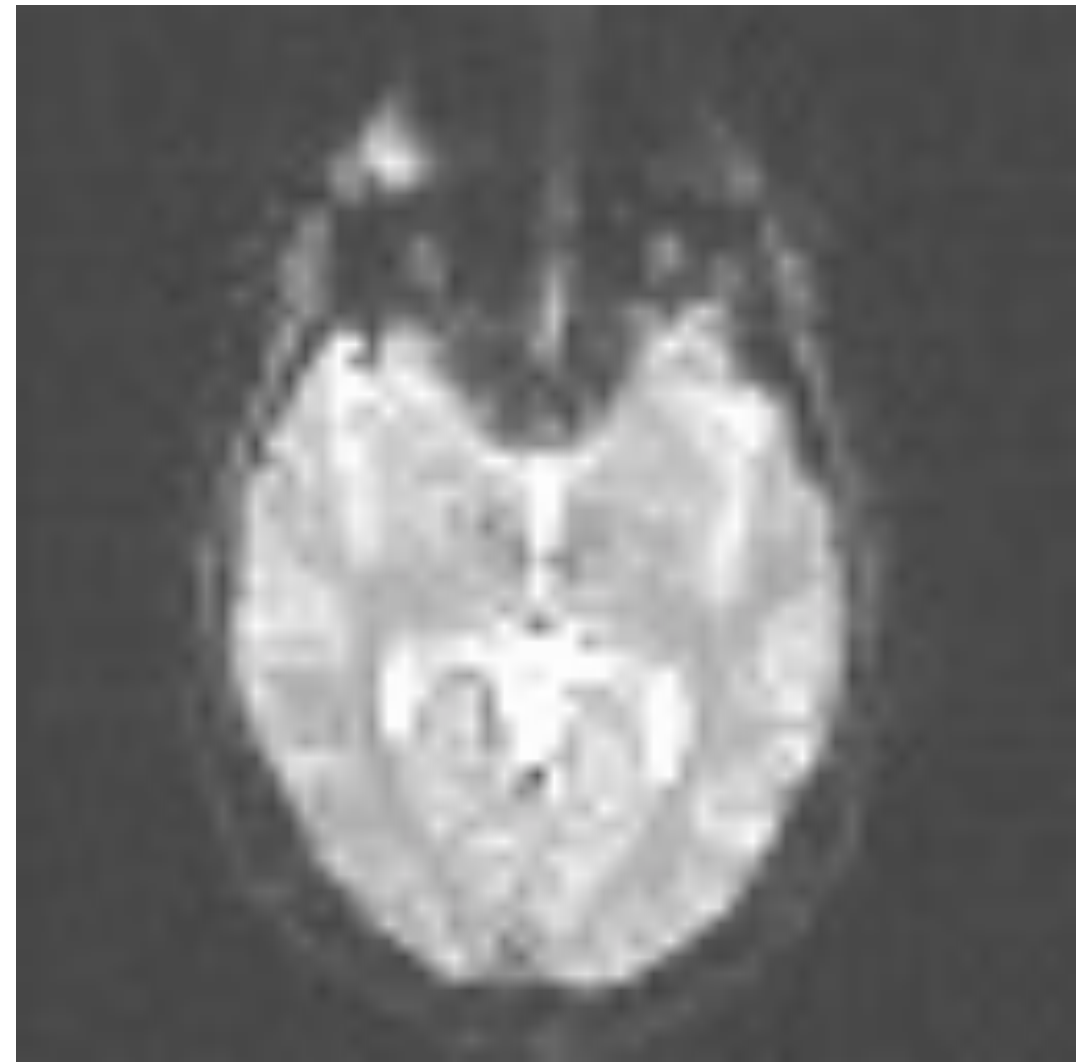
0.7 mm, 10 min  
7T, Rcv Array

Attainable SNR, CNR, resolution, speed  
depend on hardware

# Speed vs Image Artifacts



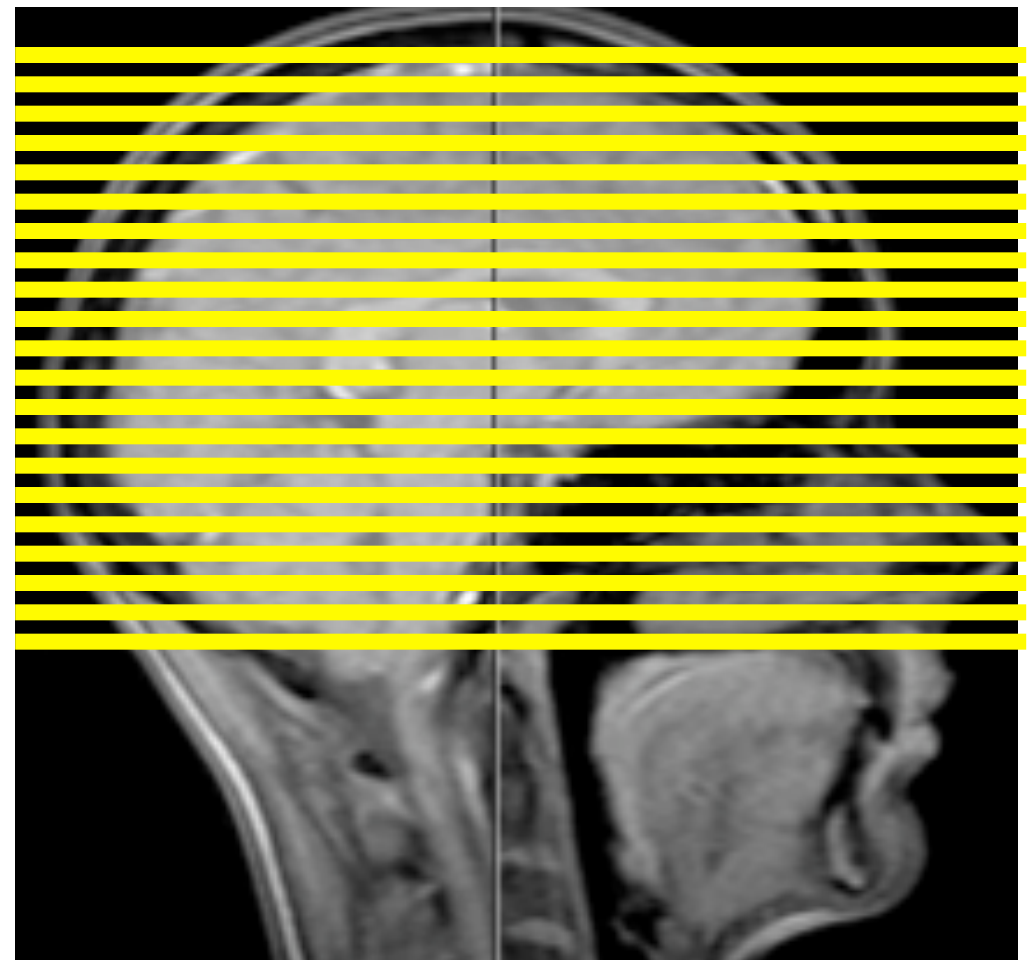
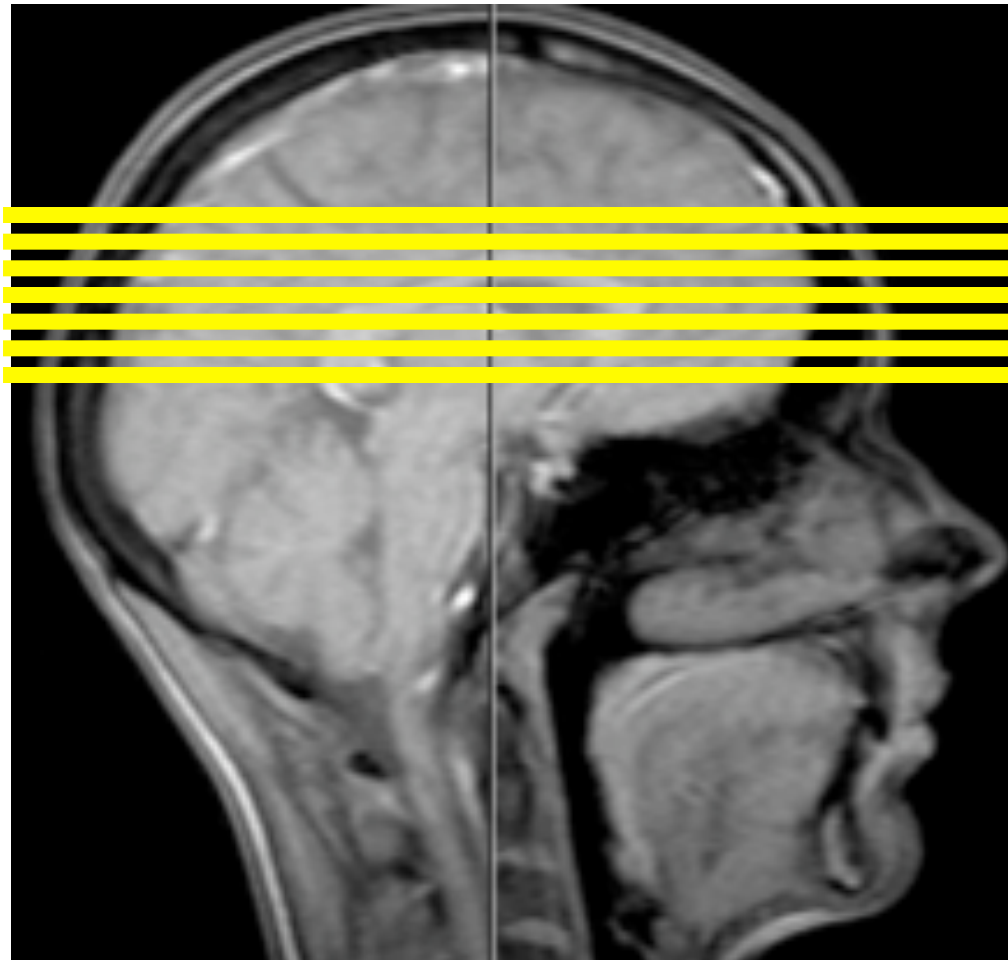
1 mm, 10 min



3 mm, 2 s

See Vinai's lecture next week.

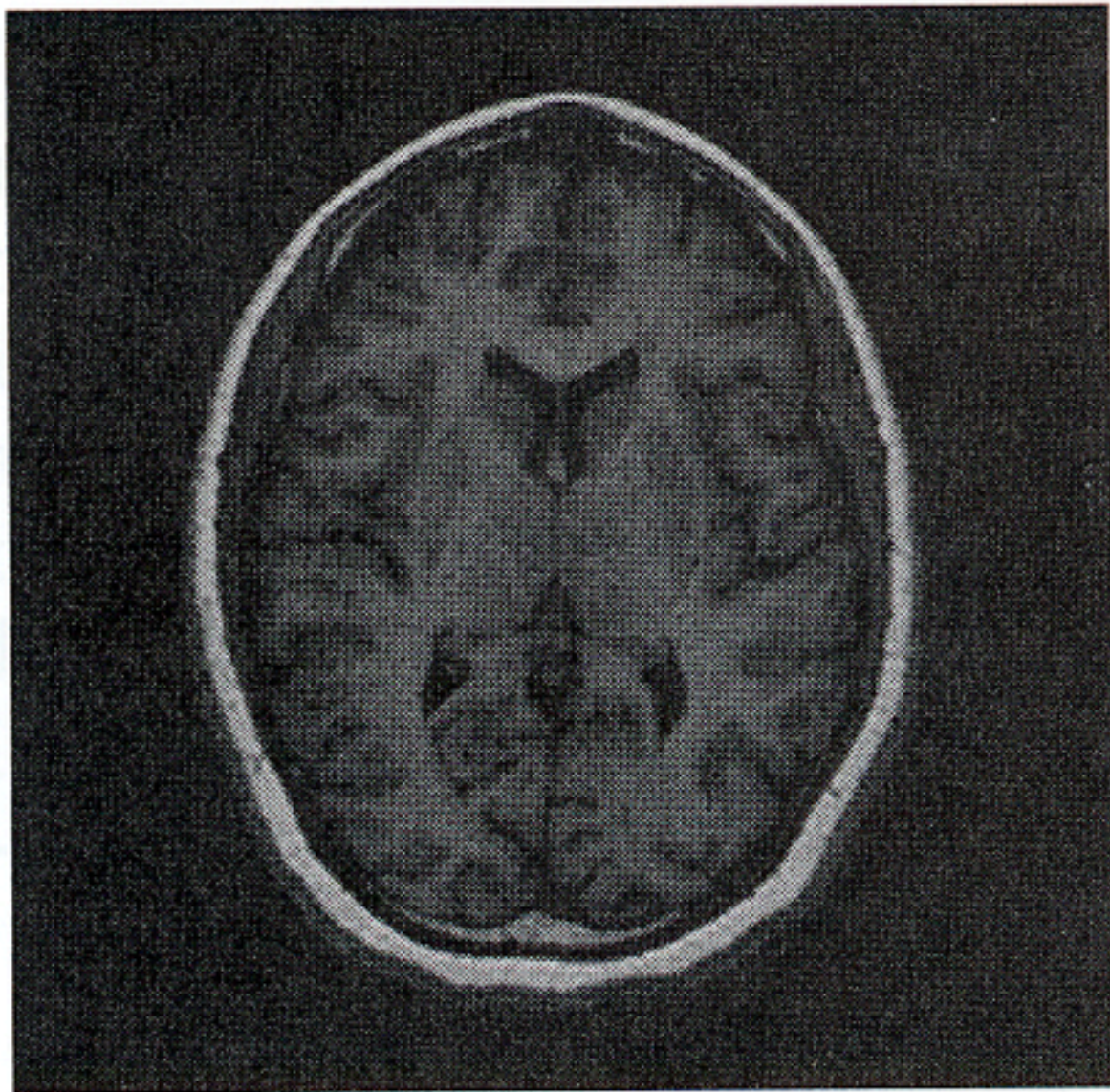
# Speed vs Coverage



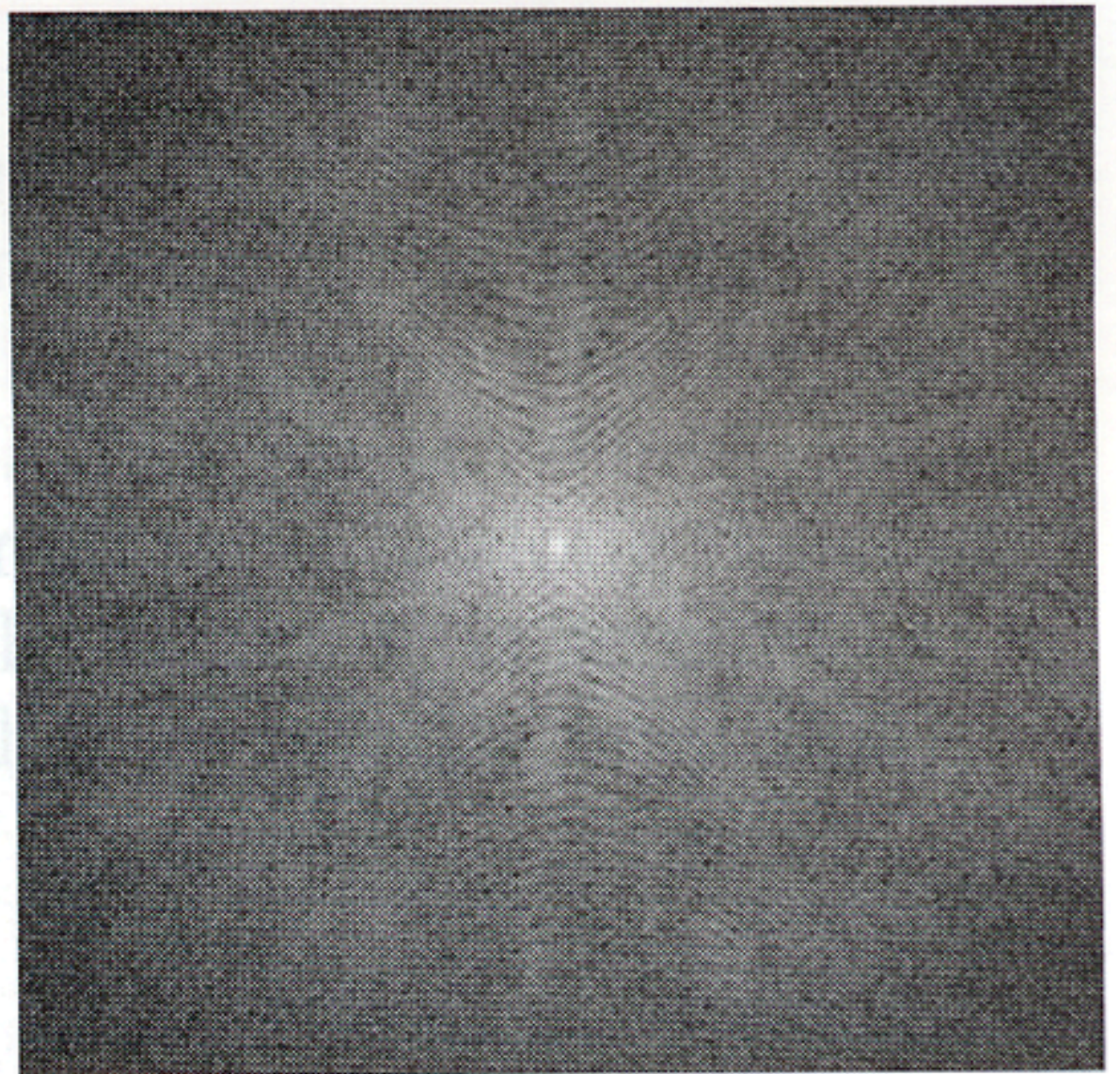
Increasing number of slices costs time



# Speed vs Resolution



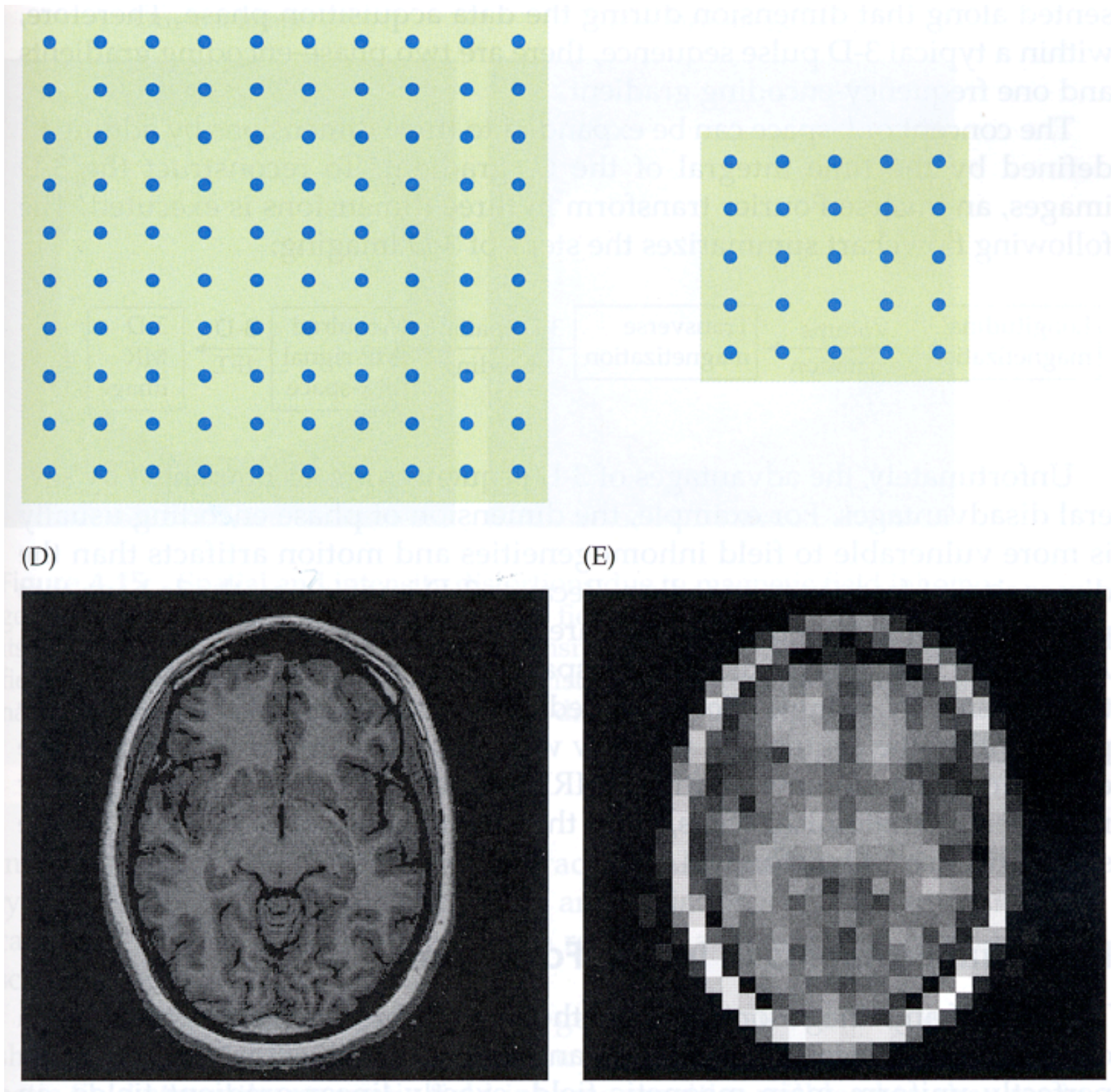
Image



k-space

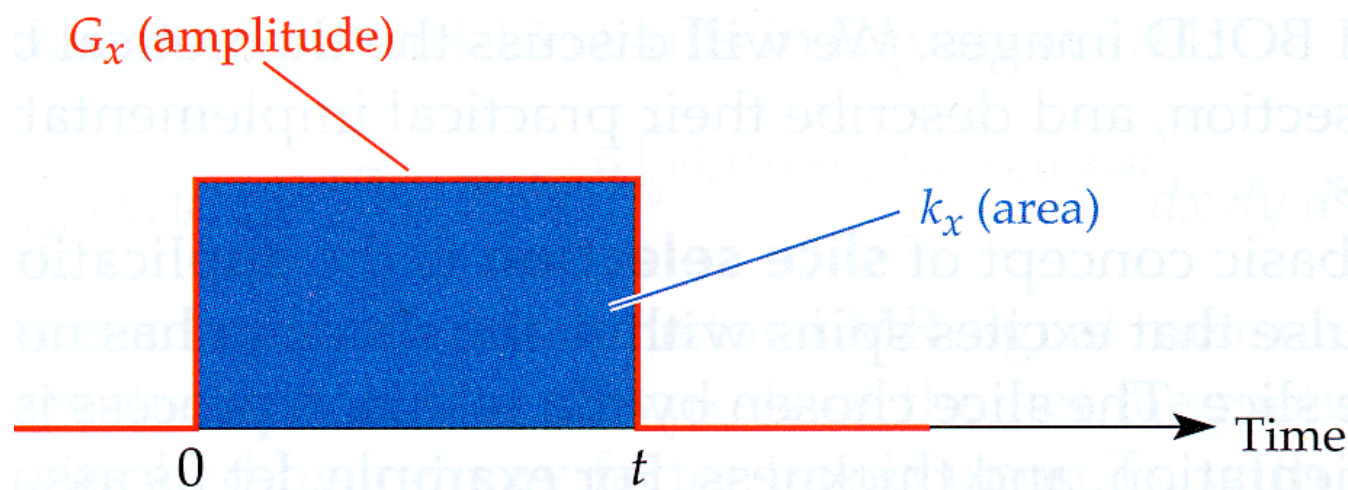


# Speed vs Resolution



# Speed vs Resolution

Increasing number of pixels costs time



The k number:

$$k_x \equiv \gamma \int_0^t G_x(\tau) d\tau$$

# Signals and Noises

- Signal amplitude depends on many things
  - Acquisition parameters
  - Tissue properties (T1, T2)
  - Hardware, e.g. field strength, coil sensitivity
- Noise amplitude depends on many things
  - electrical: coils, receivers, amps
  - mechanical: vibration
  - physiological: respiration, subject motion, cognitive



# Simple model of noise

## **Additive**

$$d(j) = s(j) + n(j)$$

## **Independent**

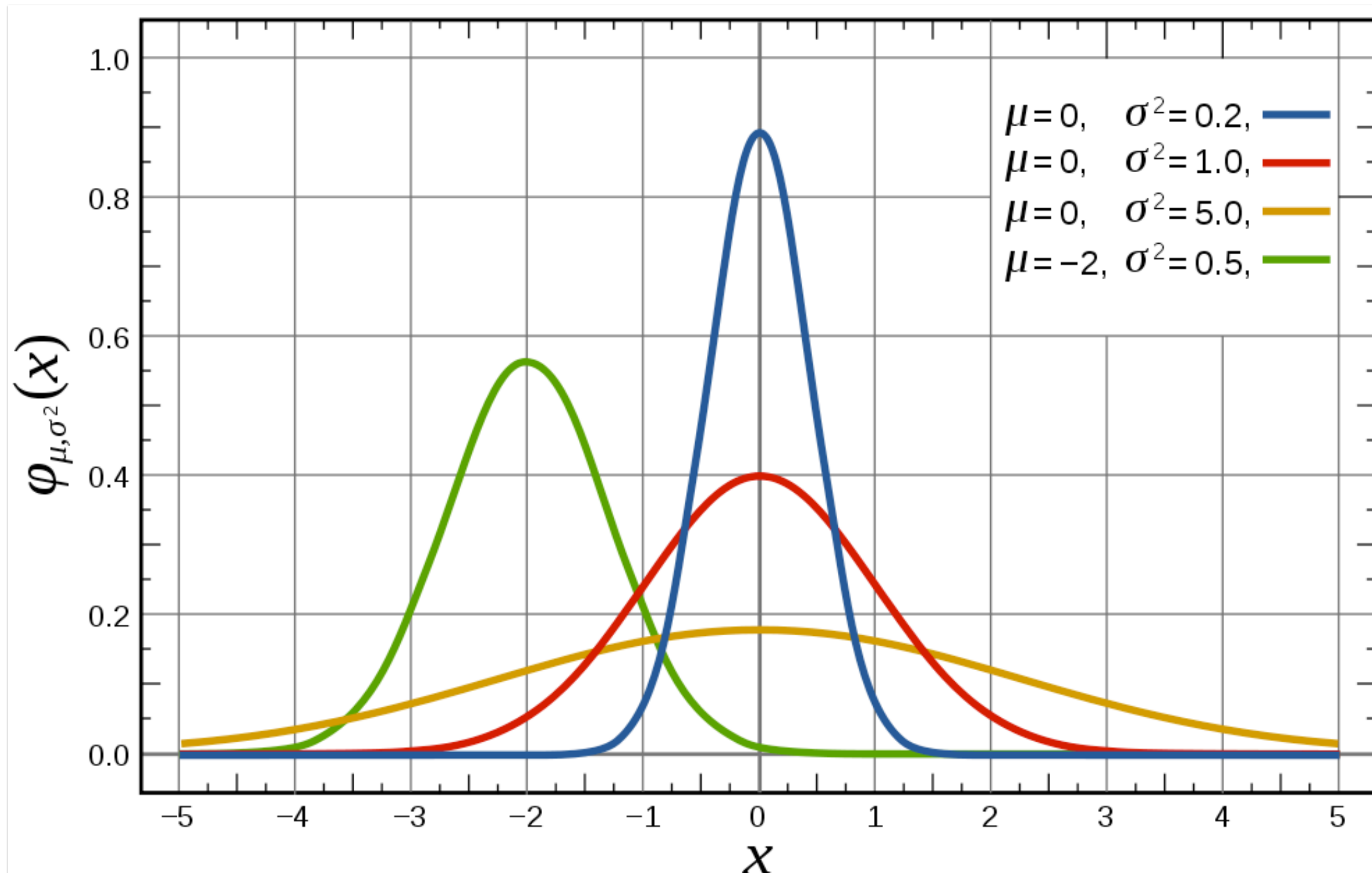
noise at  $j$  is independent of noise at other times

## **Normally distributed**

drawn from a normal distribution with 0 mean

# Simple model of noise

## Normal distribution (Gaussian)



# Simple model of noise

- If noise is sum of many Gaussian noise sources then total noise is also Gaussian - variances add
- If the number of measurements becomes large, the noise distribution looks Gaussian
- If noise is not Gaussian, then often a transformed version of the data is

Thinking about additive Gaussian noise gets us almost all the intuition we need

# Speed vs Accuracy

- If noise is Gaussian accuracy improves as  $1/\sqrt{N}$
- This applies to almost everything in MR
  - time, resolution, coverage, etc.
- Except for the physiological stuff and the other stuff that is not Gaussian

MATLAB Demo